

# CS 495 Spring 2018

## Midterm Exam

### Instructions:

- This exam is closed-book, closed-notes. Computers of any kind are not permitted.
- Write your final answers, tidily, in the boxes provided. Separate scratch paper will be provided — please ask if you need more.

1	(/8)	:
2	(/12)	:
3	(/9)	:
4	(/12)	:
5	(/5)	:
TOTAL	(/46)	:

## 1. Function Type Declarations (8 points):

For each of the following function definitions, correctly complete the preceding type declaration. Be sure to include any necessary class constraints.

(A)

```
mystery1 ::  
  
mystery1 x y z | x == y = x + z  
               | y == z = y + z  
               | otherwise = x + y - z
```

(B)

```
mystery2 ::  
  
mystery2 x p | p (head x) = tail x  
             | otherwise  = head x : mystery2 (tail x) p
```

(C)

```
mystery3 ::  
  
mystery3 g [] y = []  
mystery3 g (x:xs) y = g x y : mystery3 g xs y
```

(D)

```
mystery4 ::  
  
mystery4 x l = case l of [] -> x  
                  (y:ys) -> mystery4 (if x < y then x else y) ys
```

## 2. Basic Recursion (12 points):

Refer to the following function descriptions and sample call(s)/result(s), and implement them on the following page using explicit recursion. Unless otherwise indicated you should not use any built-in functions other than those for basic arithmetic and list construction.

- (A) `swapAdj`, which takes a list and returns a list containing the original values, but where successive pairs of values are swapped. If the input list has an odd number of values, the last value will remain in its original position.

```
> swapAdj [1..10]
[2,1,4,3,6,5,8,7,10,9]

> swapAdj "abcdefg"
"badcfeg"
```

- (B) `collatz`, which takes a positive integer  $n$  and returns the *Collatz sequence* starting at  $n$  as a list. The next value in the Collatz sequence for an even number  $n$  is  $n/2$ , while the next value for an odd number  $n$  (where  $n > 1$ ) is  $3 \times n + 1$ ; the sequence ends on the number 1.

```
> collatz 6
[6,3,10,5,16,8,4,2,1]

> collatz 32
[32,16,8,4,2,1]
```

- (C) `chunksOf`, which takes a positive integer  $n$  and a list and returns that list split into chunks of size  $n$ . If  $n$  does not divide the length of the input list evenly, then the last element of the result will be short. You may use the `take` and `drop` functions, whose behavior are also demonstrated below.

```
> chunksOf 2 [1..10]
[[1,2],[3,4],[5,6],[7,8],[9,10]]

> chunksOf 3 "hello world"
["hel","lo ","wor","ld"]

> take 3 "aloha"
"alo"

> drop 3 "aloha"
"ha"

> take 10 [1..5]
[1,2,3,4,5]

> drop 10 [1..5]
[]
```

```
swapAdj :: [a] -> [a]
```

```
collatz :: Integer -> [Integer]
```

```
chunksOf :: Int -> [a] -> [[a]]
```

### 3. Evaluating Folds (9 points):

Show the result of evaluating each of the following expressions involving either `foldr` or `foldl`.

(A) `foldl (\r x -> [x] ++ r) [] [1..10]`

(B) `foldr iter ([],0) [1..5]`  
where `iter x (y,z) = (x+z:y, x+z)`

(C) `foldr iter ([],1) "CS 495 P P P"`  
where `iter ' ' (r,n) = (0:r,n+1)`  
`iter _ (r,n) = (n:r,n)`

#### 4. Using Folds (12 points):

Refer to the following function descriptions and sample call(s)/result(s), and implement them on the following page using either `foldr` or `foldl`. You should not use explicit recursion, and unless otherwise indicated you should not use any built-in functions other than those for basic arithmetic and list construction.

- (A) `cluster`, which takes a list and returns a list of lists where each sublist contains elements that are equal and were adjacent in the original list.

```
> cluster "Mississippi"
["M","i","ss","i","ss","i","pp","i"]

> cluster "aabbccccc"
["aa", "bbb", "cccc"]
```

- (B) `intersperse`, which takes an element and a list and “intersperses” that element between the elements of the list.

```
> intersperse ',' "abcde"
"a,b,c,d,e"

> intersperse 0 [1..5]
[1,0,2,0,3,0,4,0,5]
```

- (C) `closest`, which takes a number  $n$  and a list and returns the number from the list closest in value to  $n$ . If there is a tie, the number nearest to the head of the list is returned. You may use the function `abs`, which returns the absolute value of its argument.

```
> closest 5 [1.5, 2.9, 4.8, 8.9, 6.2]
4.8

> closest 2 [6, 5, 3, 8, 9, 1, 7]
3
```

```
cluster :: (Eq a) => [a] -> [[a]]
```

```
intersperse :: a -> [a] -> [a]
```

```
closest :: (Num a, Ord a) => a -> [a] -> a
```

## 5. Universal Property of Folds (5 points):

Consider the following recursive function:

```
foo f [] = 0
foo f (x:xs) = foo f xs + (if f x then 1 else 0)
```

Using the universal property of fold, redefine `foo` using `foldr`. If your final answer is not correct, showing your derivation may earn partial credit.